

⑥ Weak neutral currents

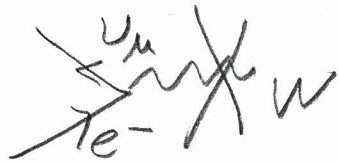
So far we have discussed weak interactions in which there is a change of electric charge ± 1 between the fermions in the vertex $\equiv$ weak charge current.

In 1973 some processes involving ν 's were observed

$$\nu_\mu e^- \rightarrow \nu_\mu e^-$$

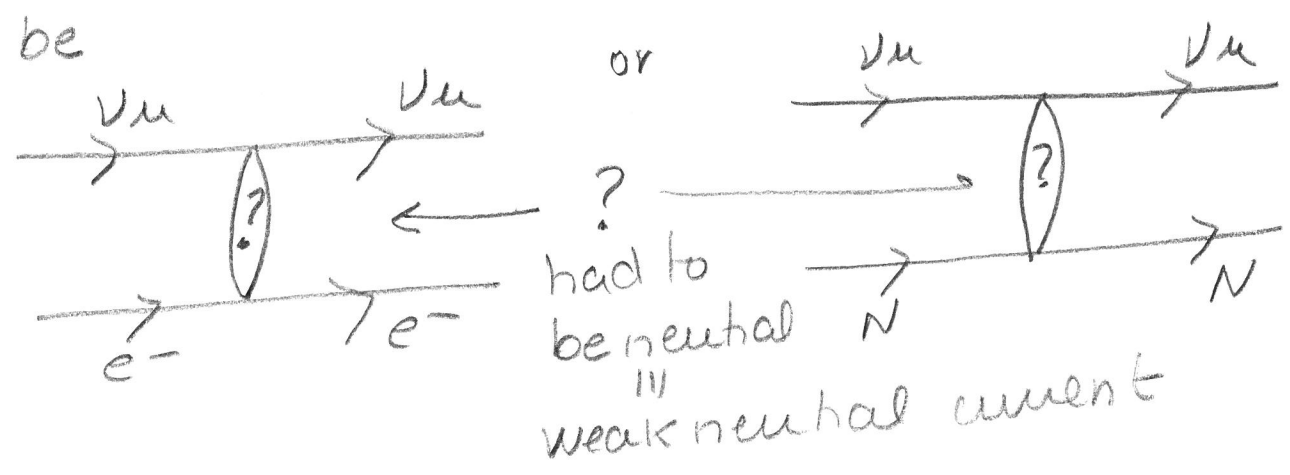
$$\nu_\mu \underset{\substack{\text{p, n}}}{N} \rightarrow \nu_\mu N$$

Since ν 's do not have electric charge nor colour these processes had to be due to weak int.
But weak interactions of fermions do not change flavour (in limit $m_\nu \rightarrow 0$) so



Further more in $\nu_\mu N \rightarrow \nu_\mu N$ there is no charge lepton

So the amplitudes for these processes had to be



the observed cross sections and many other similar weak neutral current would explain with same G_F as μ dec amplitudes e^- or q .

$\downarrow$ constant ≈ 1

$$\mathcal{M}(\nu_\mu f \rightarrow \nu_\mu f) = -\frac{8G_F}{\sqrt{2}} \rho [\bar{u}_{\nu_\mu} \gamma^\alpha (1-\gamma_5) u_{\nu_\mu}] \times [\bar{u}_f \gamma_\alpha (C_L^f \frac{1-\gamma_5}{2} + C_R^f \frac{1+\gamma_5}{2}) u_f]$$

with

f	C_L^f	C_R^f	Q_f
ν	$1/2$	0	0
e	-0.27	0.23	-1
u	0.35	-0.15	$2/3$
d	-0.43	-0.07	$-1/3$

$$\begin{aligned} C_R^f &= -Q_f \times \\ C_L^{\nu u} &= \frac{1}{2} - Q_f \times \\ C_R^{e,d} &= -\frac{1}{2} - Q_f \times \end{aligned}$$

with $x \approx 0.22-0.23$

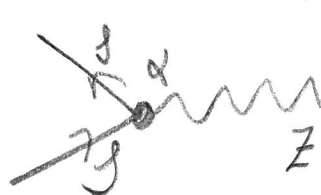
These amplitudes can be understood in terms of an effective interaction with

- interaction is mediated by a neutral vector Z^μ
- Z has a mass M_Z

So the effective Lagrangian ^{coupling constant}

$$\mathcal{L}^{NC} = - \sum_{f=u,d,e} g_Z \bar{\Psi}_f \gamma^\alpha (C_L^f P_L + C_R^f P_R) \Psi_f Z_\alpha$$

So the FR for this int'ach



$$-ig_Z \gamma^\alpha \left[C_L^f \frac{(1-\gamma_5)}{2} + C_R^f \frac{(1+\gamma_5)}{2} \right]$$

Z^μ external lines

- Z incoming
- Z outgoing



Since $M_Z \neq 0$
 $\lambda = \pm 1, 0$

$$E_\lambda^\alpha(q)$$

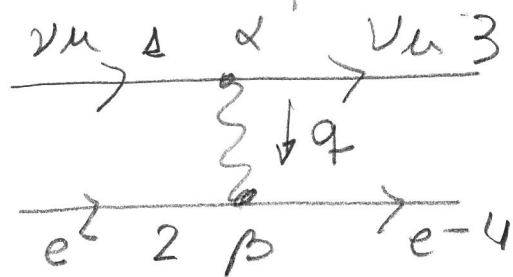
$$E_\lambda^{\alpha*}(q)$$

Z propagator



$$-i \frac{g_\alpha g_\beta - \frac{q_\alpha q_\beta}{M_Z^2}}{q^2 - M_Z^2}$$

For example



$$M = g_Z^2 \left[\bar{u}_{\nu\mu}^3 \gamma^\alpha C_L^{\nu} \left(\frac{1-\gamma_5}{2} \right) u_{\nu\mu}^1 \right] \frac{g_{\alpha\beta} - \frac{q_\alpha q_\beta}{M_Z^2}}{q^2 - M_Z^2} \left[\bar{u}_e^4 \left(C_L^e \frac{(1-\gamma_5)}{2} + C_R^e \frac{(1+\gamma_5)}{2} \right) u_e^2 \right]$$

$$\xrightarrow{q^2 \ll M_Z^2} -\frac{g_Z^2}{M_Z^2} [\bar{u}_{\nu\mu}^3 \gamma^\alpha u_{\nu\mu}^1] [\bar{u}_e^4 \gamma_\alpha u_e^2]$$

$$\Rightarrow \frac{8 G_F}{\sqrt{2}} \rho = \frac{g_Z^2}{M_Z^2}$$

and in CC $\frac{G_F}{\sqrt{2}} = \frac{g_W^2}{8 M_W^2}$

$$\Rightarrow \frac{g_W^2}{M_W^2} \rho = \frac{g_Z^2}{M_Z^2}$$

and since $\rho \simeq 1$

$$\frac{M_W^2}{M_Z^2} \sim \frac{g_W^2}{g_Z^2}$$

$\Rightarrow$ the masses and couplings of the weak CC and NC come in the same ratio.
(?)

We have written $\mathcal{L}^{NC}$ for the 1st generation

For 3 generations we can make 3 copies.

This opens up the issue of generation mixing

Let us write $\mathcal{L}^{NC}$ in the prime basis in which

the couplings are generation diagonal

$$\mathcal{L}_{quarks}^{NC} = -g_Z \sum_{i=1}^3 \bar{u}_i \gamma^\alpha [C_L^u P_L + C_R^u P_R] u_i + \bar{d}_i \gamma^\alpha [C_L^d P_L + C_R^d P_R] d_i$$

notice that $C_{L,R}^{u,d}$ are the same for the 3 generations
we can write this as

$$\mathcal{L}_{quarks}^{NC} = -g_Z (\bar{d}', \bar{s}', \bar{b}') \gamma^\alpha \left[C_L^d \begin{pmatrix} 1 & & \\ & 1 & \\ & & 1 \end{pmatrix} + C_R^d \begin{pmatrix} 1 & & \\ & 1 & \\ & & 1 \end{pmatrix} \right] \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}$$

and rotating to mass basis

$$= -g_Z (d, s, b) \underbrace{\left[U^\dagger \gamma^\alpha [C_L^d I_{3 \times 3} + C_R^d I_{3 \times 3}] U \right]}_{\gamma^\alpha [C_L^d \underbrace{U^\dagger U}_{I_{3 \times 3}} + C_R^d \underbrace{U^\dagger U}_{I_{3 \times 3}}]} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$\Rightarrow$ no generation mixing

So there is no generation mixing in NC
weak interaction $\equiv$ GIM mechanism

ⁱⁿ
Glashow, Iliopoulos and Maiani

Notice that for this to happen we need to
consider full generations (1 up and one down
quark per generation).

But when NC were discovered we only have observed
3 quarks (u, d, s). So the observation of no
flavour changing NC would not be easily
explained.

GIM realized that they could explain it if
they postulated the existence of a 4th quark
with $Q = Q_u = +\frac{2}{3}$.

In 1974 the $J/\psi \equiv$ meson made of these
4th "charm" quark and antiquark $c\bar{c}$
was discovered!