

# NEUTRINOS

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San Feliu, June 2004

## **Plan of Lectures**

**I. Standard Neutrino Properties and Mass Terms (Beyond Standard)**

**II. Neutrino Oscillations**

**III. The Data and Its Interpretation**

**IV. Some Missing Pieces and The Meaning of All This**

# Plan of Lecture I

## Standard Neutrino Properties and Mass Terms (Beyond Standard)

Introduction

Neutrinos in the SM

Neutrino Properties:

*Helicity versus Chirality, Majorana versus Dirac*

Neutrino Mass Terms Beyond the SM:

*Dirac, Majorana, the See-Saw Mechanism, Lepton Mixing*

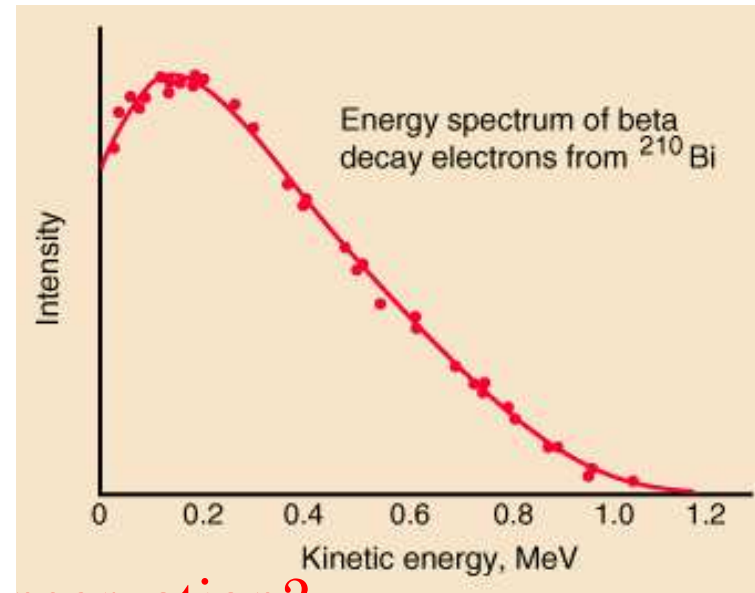
Direct Probes of Neutrino Mass Scale

## Discovery of $\nu$ 's

- At end of 1800's radioactivity was discovered and three types identified:  $\alpha$ ,  $\beta$ ,  $\gamma$   
 $\beta$  : an electron comes out of the radioactive nucleus.
- Energy conservation  $\Rightarrow e^-$  should have had a fixed energy

$$(A, Z) \rightarrow (A, Z + 1) + e^- \Rightarrow E_e = M(A, Z + 1) - M(A, Z)$$

But 1914 **James Chadwick** showed that **the electron energy spectrum is continuous**



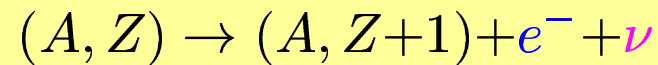
**Do we throw away the energy conservation?**

## Discovery of $\nu$ 's

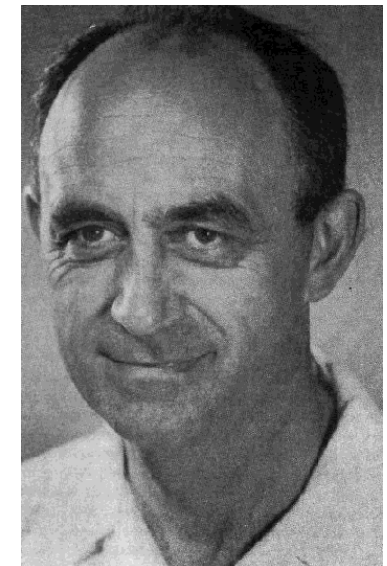
- The idea of the **neutrino** came in 1930, when **W. Pauli** tried a desperate saving operation of "the energy conservation principle".



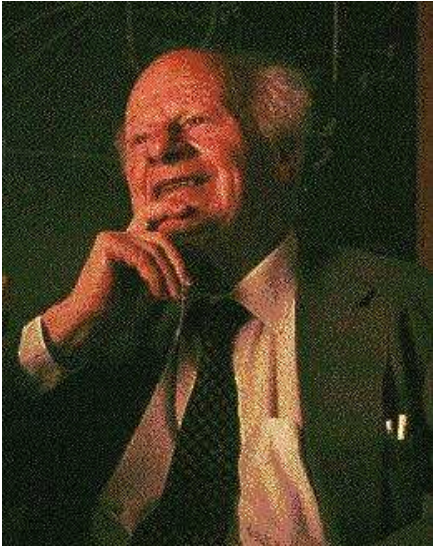
In his letter addressed to the "Liebe Radioaktive Damen und Herren" (Dear Radioactive Ladies and Gentlemen), the participants of a meeting in Tübingen. He put forward the hypothesis that a new particle exists as "constituent of nuclei", the "neutron"  $\nu$ , able to explain the continuous spectrum of nuclear beta decay



- The  $\nu$  is **light** (in Pauli's words: "the mass of the  $\nu$  should be of the same order as the  $e$  mass"), **neutral** and has **spin 1/2**
- In order to distinguish them from heavy neutrons, **Fermi** proposed to name them **neutrinos**.

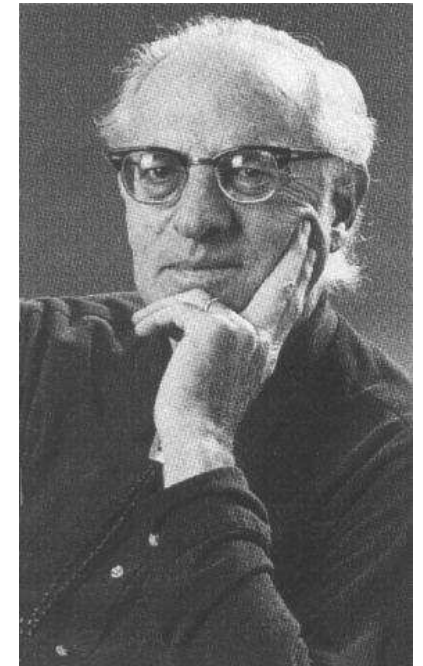


## First Detection of $\nu$ 's

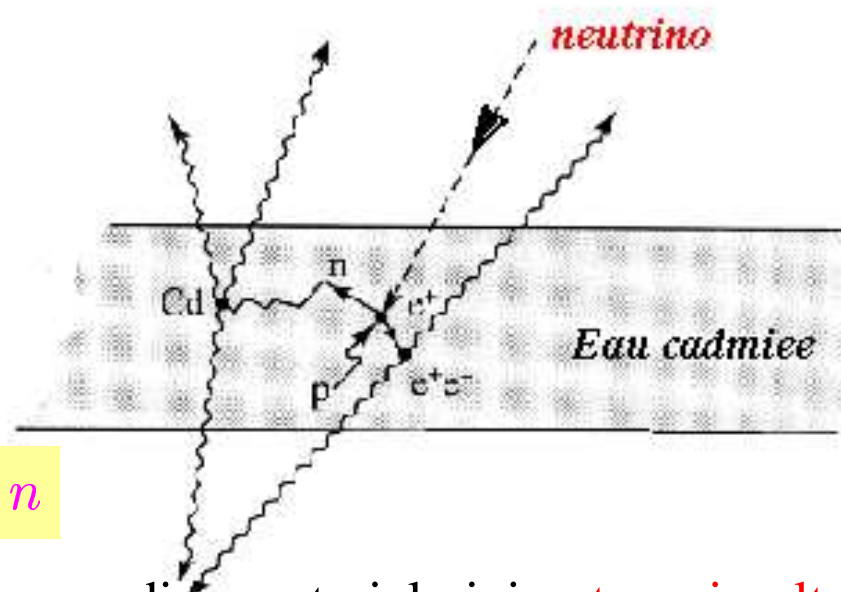


In 1934, **Hans Bethe** and **Rudolf Peierls** showed that the cross section between  $\nu$  and matter should be so small that a  $\nu$  go through the Earth without deviation

In 1953 **Frederick Reines** and **Clyde Cowan** place a neutrino detector near a nuclear plant



400 liters of water  
and cadmium chloride.



$e^+$  annihilates  $e^-$  of the surrounding material giving **two simultaneous  $\gamma$ 's**.

**neutron** captured by a cadmium nucleus with emission of  $\gamma$ 's some **15 msec after**

**The neutrino was there. Its tag was clearly visible**

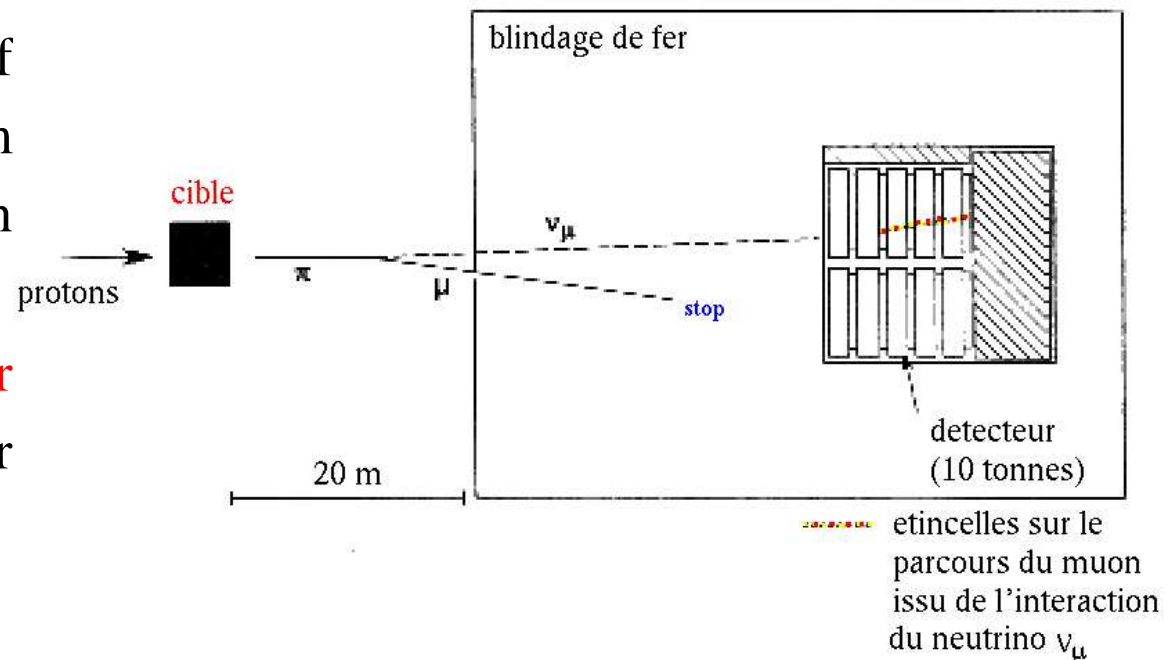
## The Other Flavours

$\nu$  coming out of a nuclear reactor is  $\bar{\nu}_e$  because it is emitted together with an  $e^-$

**Question:** Is it different from the muon type neutrino  $\nu_\mu$  that could be associated to the muon? Or is this difference a theoretical arbitrary convention?

In 1959 **M. Schwartz** thought of producing an intense  $\nu$  beam from  $\pi$ 's decay (produced when a proton beam of GeV energy hits matter)

**Schwartz, Lederman, Steinberger** and **Gaillard** built a spark chamber (a 10 tons of neon gas) to detect  $\nu_\mu$



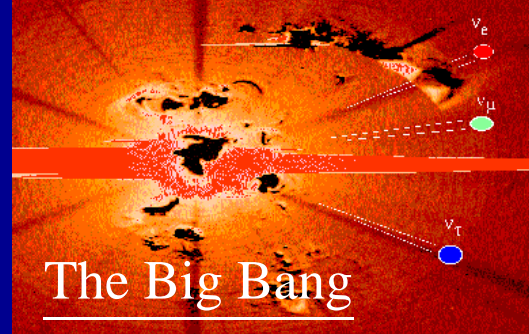
They observe 40  $\nu$  interactions: in 6 an  $e^-$  comes out and in 34 a  $\mu^-$  comes out.

If  $\nu_\mu \equiv \nu_e \Rightarrow$  equal numbers of  $\mu^-$  and  $e^- \Rightarrow$  **Conclusion:  $\nu_\mu$  is a different particle**

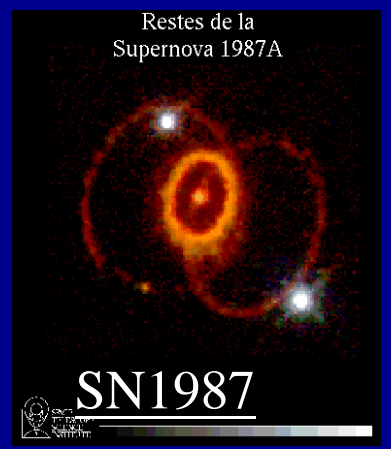
In 1977 **Martin Perl** discovers the particle tau  $\equiv$  the third lepton family.

The  $\nu_\tau$  was observed by **DONUT** experiment at FNAL in 1998 (officially in Dec. 2000).

# Sources of $\nu$ 's



The Big Bang  
 $\rho_\nu = 330/\text{cm}^3$   
 $E_\nu = 0.0004 \text{ eV}$



Restes de la  
Supernova 1987A  
**SN1987**  
 $E_\nu \sim \text{MeV}$

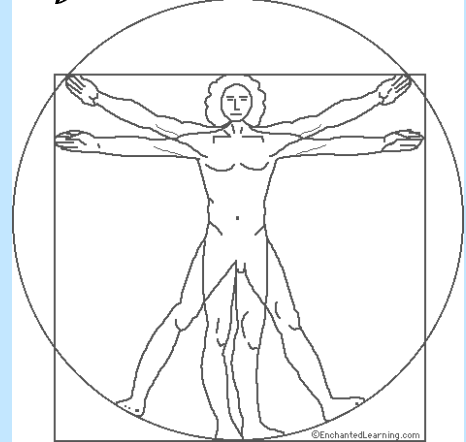


## The Sun

$\nu_e$   
 $\Phi_\nu^{\text{Earth}} = 6 \times 10^{10} \nu/\text{cm}^2\text{s}$   
 $E_\nu \sim 0.1\text{--}20 \text{ MeV}$

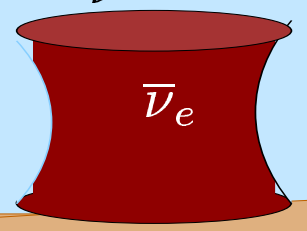
## Human Body

$\Phi_\nu = 340 \times 10^6 \nu/\text{day}$



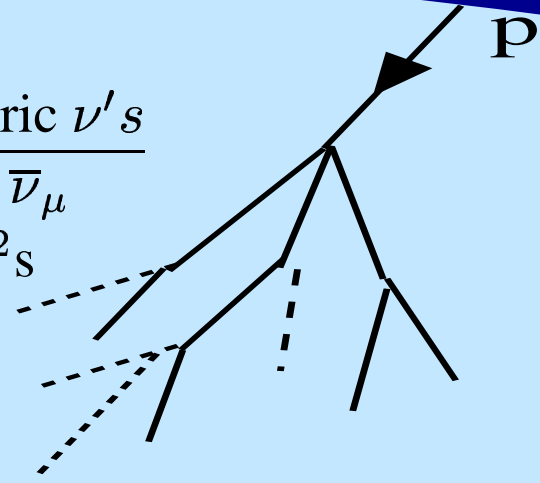
## Nuclear Reactors

$E_\nu \sim \text{few MeV}$



## Atmospheric $\nu$ 's

$\nu_e, \nu_\mu, \bar{\nu}_e, \bar{\nu}_\mu$   
 $\Phi_\nu \sim 1 \nu/\text{cm}^2\text{s}$



## Earth's radioactivity

$\Phi_\nu \sim 6 \times 10^6 \nu/\text{cm}^2\text{s}$

## Accelerators

$E_\nu \simeq 0.3\text{--}30 \text{ GeV}$





## $\nu$ in the SM

- The SM is a gauge theory based on the symmetry group

$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

- LEP tested this symmetry to 1% precision and the missing particles  $t, \nu_\tau$

$(1, 2)_{-\frac{1}{2}}$	$(3, 2)_{\frac{1}{6}}$	$(1, 1)_{-1}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$\begin{pmatrix} u^i \\ d^i \end{pmatrix}_L$	$e_R$	$u^i_R$	$d^i_R$
$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L$	$\begin{pmatrix} c^i \\ s^i \end{pmatrix}_L$	$\mu_R$	$c^i_R$	$s^i_R$
$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$	$\begin{pmatrix} t^i \\ b^i \end{pmatrix}_L$	$\tau_R$	$t^i_R$	$n^i_R$

Notice there is no  $\nu_R$

$\Rightarrow$  Accidental global symmetry:

$$B \times L_e \times L_\mu \times L_\tau$$

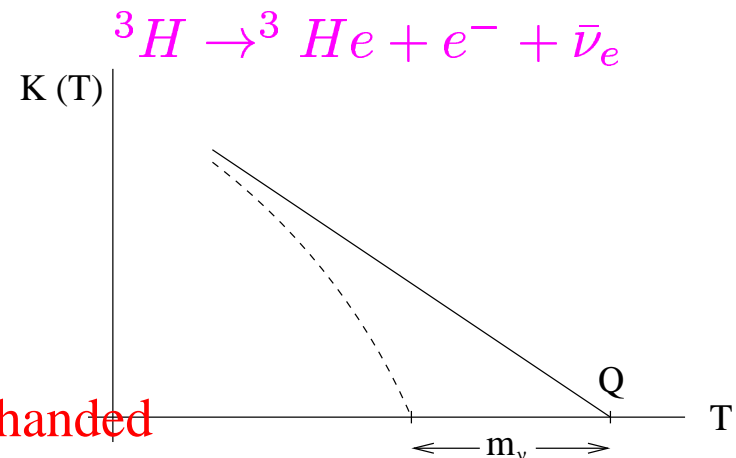
- When SM was invented upper bounds on  $m_\nu$

$$m_{\nu_e} < 2.2 \text{ eV}$$

$$m_{\nu_\mu} < 190 \text{ KeV} \quad (\pi \rightarrow \mu \nu_\mu)$$

$$m_{\nu_\tau} < 18.2 \text{ MeV} \quad (\tau \rightarrow n \pi \nu_\tau)$$

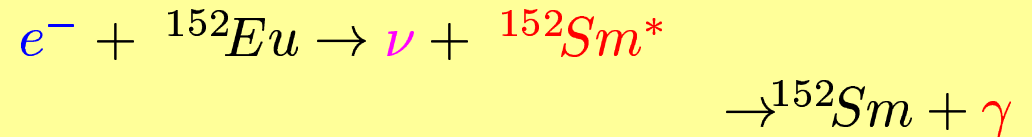
- Neutrinos are conjured to be massless and left-handed



# Neutrino Helicity

- The neutrino helicity was measured in 1957 in a experiment by Goldhaber et al.

- Using the electron capture reaction



with  $J({}^{152}\text{Eu}) = J({}^{152}\text{Sm}) = 0$  and  $L(e^-) = 0$

- Angular momentum conservation  $\Rightarrow$ 

$$\begin{cases} J_z(e^-) &= J_z(\nu) + J_z(\text{Sm}^*) \\ &= J_z(\nu) + J_z(\gamma) \\ +\frac{1}{2} &= -\frac{1}{2} \quad +1 \Rightarrow J_z(\nu) = -\frac{1}{2}J_z(\gamma) \end{cases}$$

- Nuclei are heavy  $\Rightarrow \vec{p}({}^{152}\text{Eu}) \simeq \vec{p}({}^{152}\text{Sm}) \simeq \vec{p}({}^{152}\text{Sm}^*) = 0$

So momentum conservation  $\Rightarrow \vec{p}(\nu) = -\vec{p}(\gamma) \Rightarrow \nu \text{ helicity} = \gamma \text{ helicity}$

- Goldhaber et al found  $\gamma$  had negative helicity  $\Rightarrow \nu$  has helicity  $-1$

Thus so far  $\nu$  was a particle with  $m_\nu = 0$  and left handed.

(because for massless fermions helicity  $\equiv$  chirality...)

## Helicity versus Chirality

- The Lagrangian of a massive free fermion  $\psi$  is  $\mathcal{L} = \bar{\psi}(x)(i\gamma \cdot \partial - m)\psi(x)$

- The Equation of Motion is:  $i\frac{\partial}{\partial t}\psi = H\psi = \gamma^0(\vec{\gamma} \cdot \vec{p} + m)\psi$

- In momentum space this equation has 4 possible solutions

$$(\gamma \cdot p - m)u_s(\vec{p}) = 0$$

$$(\gamma \cdot p + m)v_s(\vec{p}) = 0$$

$s = \pm\frac{1}{2}$  and  $u_s(\vec{p})$  and  $v_s(\vec{p})$  are the four component Dirac spinors.

- For this free fermion  $[H, \vec{J}] = 0$  and  $[\vec{p}, \vec{J} \cdot \vec{p}] = 0$  with  $\vec{J} = \vec{L} + \frac{\vec{\sigma}}{2}$  ( $\sigma^i = -\gamma^0 \gamma^5 \gamma^i$ )

$\Rightarrow$  we can choose  $u_s(\vec{p})$  and  $v_s(\vec{p})$  to be eigenstates also of the helicity projector

$$P_{\pm} = \frac{1 \pm 2\vec{J} \cdot \frac{\vec{p}}{|\vec{p}|}}{2} = \frac{1 \pm \vec{\sigma} \cdot \frac{\vec{p}}{|\vec{p}|}}{2}$$

So the helicity states can be chosen as physical states for free fermions

## Helicity versus Chirality

- We define the **chiral** projections  $P_{R,L} = \frac{1 \pm \gamma_5}{2}$

$$\psi = \psi_L + \psi_R \quad \psi_L = \frac{1 - \gamma_5}{2} \psi \quad \psi_R = \frac{1 + \gamma_5}{2} \psi$$

- In the SM the neutrino interaction terms

$$\mathcal{L}_{int} = \frac{ig}{\sqrt{2}} [j_\mu^+ W_\mu^- + j_\mu^- W_\mu^+] + \frac{ig}{\sqrt{2} \cos \theta_W} j_\mu^Z Z_\mu$$

$$j_\mu^- = \bar{l}_\alpha \gamma_\mu P_L \nu_\alpha \quad \alpha = e, \mu, \tau \quad j_\mu^+ = j_\mu^{-\dagger} \quad j_\mu^Z = \bar{\nu}_\alpha \gamma_\mu P_L \nu_\alpha$$

$\Rightarrow \nu_L$  interact and  $\nu_R$  do not interact

$\Rightarrow$  **chirality states** are **physical states** for weak interactions

- For **massless** fermions the Dirac equation can be written

$$\vec{\sigma} \cdot \vec{p} \psi = -\gamma^0 \gamma^5 \vec{\gamma} \cdot \vec{p} \psi = -\gamma^0 \gamma^5 \gamma^0 E \psi = \gamma^5 E \psi \Rightarrow \text{For } m = 0 \quad P_\pm = P_{R,L}$$

$\Rightarrow$  **Helicity** and **chirality** states are the same for **massless** fermions.

## Helicity versus Chirality

- For **massive** fermions the **chiral** states are a **combination of both helicity** states.

$$P_{R,L} = P_{\pm} + \mathcal{O}\left(\frac{m}{p}\right)$$

- Let's do the following *gedanken* experiment:
  - Set a  $\nu$  state with its spin looking down
    - (1st) Let's assume it moves up (**it has helicity -1**) till it hits a target
    - (2nd) Let's assume it moves down (**it has helicity +1**) till it hits a target
- If  $m_{\nu} = 0$ : (1) the **upgoing**  $\nu \equiv \nu_L$  produces  $e^{-}$ 
  - (2) **down** we see **nothing**
- If  $m_{\nu} \neq 0$ : (1) the **upgoing**  $\nu \equiv$  mostly  $\nu_L$  produces  $e^{-}$ 
  - (2) the **downgoing**  $\nu \equiv$  small  $\nu_L$  component produces **few**  $e^{-}$

## Dirac versus Majorana Neutrinos

- In the SM neutral bosons can be of two type:
  - Their own antiparticle such as  $\gamma, \pi^0 \dots$
  - Different from their antiparticle such as  $K^0, \bar{K}^0 \dots$

- In the SM  $\nu$  are the only *neutral fermions*

⇒ **OPEN QUESTION:** are neutrino and antineutrino the same or different particles?

\* **ANSWER 1:**  $\nu$  different from anti- $\nu$  ⇒  $\nu$  is a *Dirac* particle (like  $e$ )

⇒ It is described by a *Dirac* field  $\nu(x) = \sum_{s, \vec{p}} \left[ a_s(\vec{p}) u_s(\vec{p}) e^{-ipx} + b_s^\dagger(\vec{p}) v_s(\vec{p}) e^{ipx} \right]$

⇒ And the charged conjugate neutrino field  $\equiv$  the antineutrino field

$$\nu^C = C \nu C^{-1} = \eta_C^* \sum_{s, \vec{p}} \left[ b_s(\vec{p}) u_s(\vec{p}) e^{-ipx} + a_s^\dagger(\vec{p}) v_s(\vec{p}) e^{ipx} \right] = -\eta_C^* C \bar{\nu}^T$$

$(C = i\gamma^2 \gamma^0)$

which contain two sets of creation–annihilation operators

⇒ These two fields can be rewritten in terms of 4 chiral fields

$$\nu_L, \nu_R, (\nu_L)^C, (\nu_R)^C \quad \text{with} \quad \nu = \nu_L + \nu_R \quad \text{and} \quad \nu^C = (\nu_L)^C + (\nu_R)^C$$

# Dirac versus Majorana Neutrinos

\* ANSWER 2:  $\nu$  same as anti- $\nu$   $\Rightarrow \nu$  is a *Majorana* particle :  $\nu_M = \nu_M^C$

$$\Rightarrow \eta_C^* \sum_{s, \vec{p}} \left[ b_s(\vec{p}) u_s(\vec{p}) e^{-ipx} + a_s^\dagger(\vec{p}) v_s(\vec{p}) e^{ipx} \right] = \sum_{s, \vec{p}} \left[ a_s(\vec{p}) u_s(\vec{p}) e^{-ipx} + b_s^\dagger(\vec{p}) v_s(\vec{p}) e^{ipx} \right]$$

$\Rightarrow$  So we can rewrite the field  $\nu_M = \sum_{s, \vec{p}} \left[ a_s(\vec{p}) u_s(\vec{p}) e^{-ipx} + \eta_C^* a_s^\dagger(\vec{p}) v_s(\vec{p}) e^{ipx} \right]$

which contains only one set of creation–annihilation operators

$\Rightarrow$  A Majorana particle can be described with only 2 independent chiral fields:

$$\nu_L \text{ and } (\nu_L)^C \text{ which verify } \nu_L = (\nu_R)^C \quad (\nu_L)^C = \nu_R$$

• In the SM the interaction term for neutrinos

$$\mathcal{L}_{int} = \frac{ig}{\sqrt{2}} \left[ (\bar{l}_\alpha \gamma_\mu P_L \nu_\alpha) W_\mu^- + (\bar{\nu}_\alpha \gamma_\mu P_L l_\alpha) W_\mu^+ \right] + \frac{ig}{\sqrt{2} \cos \theta_W} (\bar{\nu}_\alpha \gamma_\mu P_L \nu_\alpha) Z_\mu$$

Only involves two chiral fields  $P_L \nu = \nu_L$  and  $\bar{\nu} P_R = \eta_C (\nu_L)^C C^\dagger$

$\Rightarrow$  Weak interaction cannot distinguish if neutrinos are *Dirac or Majorana*

The difference arises from *the mass term*

## $\nu$ Mass Terms

- A **fermion mass** can be seen as at a **Left-Right transition**

$$m_f \overline{f}_L f_R + h.c. \quad (\text{this is not } SU(2)_L \text{ gauge invariant})$$

- In the Standard Model mass comes from *spontaneous symmetry breaking* via Yukawa interaction of the left-handed doublet  $\psi_L$  with the right-handed singlet  $l_R$ :

$$\mathcal{L}_Y^{(\ell)} = -\frac{\sqrt{2}}{v} \overline{\psi}_{lL} M^{(\ell)} l_R \phi + h.c. \quad \phi = \text{the scalar doublet}$$

- After spontaneous symmetry breaking

$$\phi \xrightarrow{SSB} \left\{ \begin{array}{c} 0 \\ \frac{v+H}{\sqrt{2}} \end{array} \right\} \Rightarrow \mathcal{L}_{\text{mass}}^{(\ell)} = -\bar{l}_L M^{(\ell)} l_R + h.c.$$

$M^{(\ell)}$  = **Dirac mass matrix** for charged leptons

- $\nu$ 's do not participate in QED or QCD and only  $\nu_L$  is relevant for weak interactions  $\Rightarrow$  there is no *dynamical* reason for introducing  $\nu_R$ , so

**How can we generate a mass for the neutrino?**



## $\nu$ Mass Terms: Dirac Mass

### OPTION 1:

- One introduces  $\nu_R$  which can couple to the lepton doublet by Yukawa interaction

$$\mathcal{L}_Y^{(\nu)} = -\frac{\sqrt{2}}{v} \overline{\psi}_L M^{(\nu)} \nu_R \tilde{\phi} + \text{h.c.} \quad (\tilde{\phi} = i\tau_2 \phi^*)$$

- Under spontaneous symmetry-breaking,

$$\mathcal{L}_Y^{(\nu)} \Rightarrow \mathcal{L}_{\text{mass}}^{(\text{Dirac})} = -\overline{\nu}_L M_D^\nu \nu_R + \text{h.c.} \equiv -\frac{1}{2} (\overline{\nu}_L M_D^\nu \nu_R + \overline{(\nu_R)^c} M_D^{\nu T} (\nu_L)^c) + \text{h.c.}$$

$M_D^\nu$  = Dirac mass for neutrinos

- $\mathcal{L}_{\text{mass}}^{(\text{Dirac})}$  involves the four chiral fields  $\nu_L$ ,  $\nu_R$ ,  $(\nu_L)^c$ ,  $(\nu_R)^c$

$\Rightarrow$  The eigenstates of  $M_D^\nu$  are Dirac particles (same as quarks and charged leptons)

$\Rightarrow$  Total Lepton number is conserved by construction (not accidentally):

$$U(1)_L \nu = e^{i\alpha} \nu \quad \text{and} \quad U(1)_L \overline{\nu} = e^{-i\alpha} \overline{\nu}$$

$$U(1)_L \nu^c = e^{-i\alpha} \nu^c \quad \text{and} \quad U(1)_L \overline{\nu^c} = e^{i\alpha} \overline{\nu^c}$$

## $\nu$ Mass Terms: Majorana Mass

### OPTION 2:

- One **does not** introduce  $\nu_R$  but uses that the field  $(\nu_L)^c$  is right-handed, so that one can write a **Lorentz-invariant** mass term

$$\mathcal{L}_{\text{mass}}^{(\text{Maj})} = -\frac{1}{2} \bar{\nu}_L M_M^\nu \nu_L^c + \text{h.c.}$$

$M_M^\nu$  = Majorana mass for neutrinos

- But under any  $U(1)$  symmetry

$$U(1) \nu^c = e^{-i\alpha} \nu^c \quad \text{and} \quad U(1) \bar{\nu} = e^{-i\alpha} \bar{\nu}$$

$\Rightarrow$  it can only appear for particles without electric charge

$\Rightarrow$  **Total Lepton Number** is **not conserved**

$\Rightarrow$  The eigenstates of  $M_M^\nu$  are Majorana particles (verify  $\nu_i^c = \nu_i$ )

$\Rightarrow$  **But  $SU(2)_L$  gauge invariance is broken!!!**

# General $SU(2)_L$ invariant $\nu$ Mass Terms

## OPTION 3:

- Introduce  $\nu_{R_i}$  ( $i = 1, m$ ) and write all Lorentz and  $SU(2)_L$  invariant mass term

$$\mathcal{L}_Y^{(\nu)} = -\frac{\sqrt{2}}{v} \overline{\psi_{L,j}} M_{D,ji}^* \nu_{R,i} \tilde{\phi} - \frac{1}{2} \overline{\nu_{R,j}} M_{N,ji} \nu_{R,i}^c + \text{h.c.}$$

- Under spontaneous symmetry-breaking

$$\begin{aligned} \mathcal{L}_{\text{mass}}^{(\nu)} &= -\overline{\nu_{L,j}} M_{D,ji}^* \nu_{R,i} - \frac{1}{2} \overline{\nu_{R,j}} M_{N,ji} \nu_{R,i}^c + \text{h.c.} \\ &= -\frac{1}{2} (\overline{\nu_{R,j}} M_{D,ji}^T \nu_{L,i} + \overline{\nu_{L,j}^c} M_{D,ji} \nu_{R,i}^c) - \frac{1}{2} \overline{\nu_{R,j}} M_{N,ji} \nu_{R,i}^c + \text{h.c.} \\ &\equiv -\frac{1}{2} \overline{\vec{\nu}^c} M^\nu \vec{\nu} + \text{h.c.} \end{aligned}$$

with  $\vec{\nu} = \begin{pmatrix} \nu_{L,k} \\ \nu_{R,l}^c \end{pmatrix}$  and  $M^\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix}$

- In general if  $M_N \neq 0 \Rightarrow 3+m$  Majorana neutrino states (verify  $\nu_i^c = \nu_i$ )  
how many are light depends on hierarchy between  $M_D$  and  $M_N$

$\Rightarrow$  Total Lepton Number is not conserved

## The See-Saw Mechanism

- A particular realization of OPTION 3: Add 3  $\nu_{R_i}$  so

$$\begin{aligned}
 \mathcal{L}_{\text{mass}}^{(\nu)} &= -\overline{\nu_{L,j}} m_{D,ji} \nu_{R,i} - \frac{1}{2} \overline{\nu_{R,j}} M_{N,ji} \nu_{R,i}^c + \text{h.c.} \\
 &= -\frac{1}{2} (\overline{\nu_{R,j}} m_{D,ji} \nu_{L,i} + \overline{\nu_{L,j}^c} m_{D,ij} \nu_{R,i}^c) - \frac{1}{2} \overline{\nu_{R,j}} M_{N,ji} \nu_{R,i}^c + \text{h.c.} \\
 &\equiv -\frac{1}{2} \overline{\vec{\nu}^c} M^\nu \vec{\nu} + \text{h.c.}
 \end{aligned}$$

with  $\vec{\nu} = \begin{pmatrix} \nu_{L,k} \\ \nu_{R,l}^c \end{pmatrix}$  and  $M^\nu = \begin{pmatrix} 0 & m_D \\ m_D^T & M_N \end{pmatrix}$

- Assume  $M_N \gg m_D \Rightarrow$

- 3 Heavy  $\nu$ 's of mass  $m_{\nu_H} \sim M_N$
- 3 light neutrinos  $\nu$ 's of mass  $m_{\nu_l} = m_D^T M_N^{-1} m_D$
- The heavier  $\nu_H$  the lighter  $\nu_l \Rightarrow$  **See-Saw Mechanism**
- Arises in many extensions of the SM: **SO(10) GUTS, Left-right...**

# Lepton Mixing

- Charged current and mass for **3** charged leptons  $\ell_i$  and  $N$  neutrinos  $\nu_j$  in weak basis

$$\mathcal{L}_{CC} + \mathcal{L}_M = -\frac{g}{\sqrt{2}} \overline{\ell_L^W} \gamma^\mu \nu^W W_\mu^+ - \overline{\ell_L^W} M_\ell \ell_R^W - \frac{1}{2} \overline{\nu^c W} M_\nu \nu^W + \text{h.c.}$$

- Changing to mass basis by rotations

$$\ell_L^W = V_L^\ell \ell_L \quad \ell_R^W = V_R^\ell \ell_R \quad \nu^W = V^\nu \nu$$

$$V_L^{\ell\dagger} M_\ell V_R^\ell = \text{diag}(m_e, m_\mu, m_\tau) \quad V^{\nu\dagger} M_\nu^\dagger M_\nu V^\nu = \text{diag}(m_1^2, m_2^2, m_3^2, \dots, m_N^2)$$

$V_{L,R}^\ell \equiv$  Unitary **3**  $\times$  **3** matrices and  $V^\nu \equiv$  Unitary  $N \times N$  matrix.

- The charged current in the mass basis

$$\mathcal{L}_{CC} = -\frac{g}{\sqrt{2}} \overline{\ell_L^i} \gamma^\mu U_{\text{LEP}}^{ij} \nu_j W_\mu^+$$

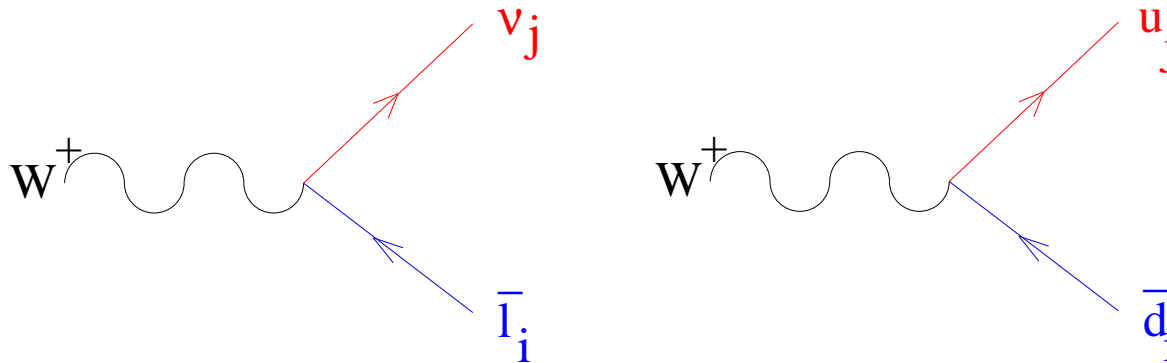
$U_{\text{LEP}} \equiv 3 \times N$  matrix

$$U_{\text{LEP}}^{ij} = \sum_{k=1}^3 V_L^{\ell\dagger ik} V^{\nu kj}$$

## Effects of $\nu$ Mass

- Neutrino masses can have kinematic effects
- Also if neutrinos have a mass the charged current interactions of leptons are not diagonal (same as quarks)

$$\frac{g}{\sqrt{2}} W_{\mu}^{+} \sum_{ij} (U_{LEP}^{ij} \bar{\ell}^i \gamma^{\mu} L \nu^j + U_{CKM}^{ij} \bar{U}^i \gamma^{\mu} L D^j) + h.c.$$



- SM gauge invariance *does not imply*  $U(1)_{L_e} \times U(1)_{L_{\mu}} \times U(1)_{L_{\tau}}$  symmetry
- Total lepton number  $U(1)_L = U(1)_{L_e + L_{\mu} + L_{\tau}}$  can be or cannot be still a symmetry depending on whether neutrinos are Dirac or Majorana

# Neutrino Mass Scale: Tritium $\beta$ Decay

- Fermi proposed a kinematic search of  $\nu_e$  mass from beta spectra in  ${}^3\text{H}$  beta decay



• For “allowed” nuclear transitions, the electron spectrum is given by phase space alone

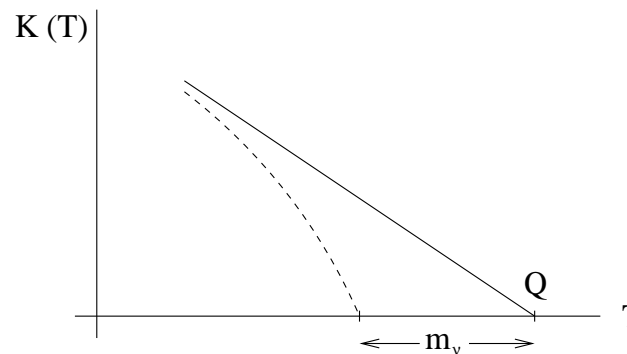
$$K(T) \equiv \sqrt{\frac{dN}{dT} \frac{1}{C_p E F(E)}} \propto \sqrt{(Q - T) \sqrt{(Q - T)^2 - m_\nu^2}}$$

$T = E_e - m_e$ ,  $Q =$  maximum kinetic energy, (for  ${}^3\text{H}$  beta decay  $Q = 18.6$  KeV)

- $m_\nu \neq 0 \Rightarrow$  distortion from the straight-line at the end point of the spectrum

$$m_\nu = 0 \Rightarrow T_{\text{max}} = Q$$

$$m_\nu \neq 0 \Rightarrow T_{\text{max}} = Q - m_\nu$$



– At present only a bound:

$$m_{\nu_e}^{\text{eff}} \equiv \sum m_j |U_{ej}|^2 < 2.2 \text{ eV} \quad (\text{at 95 \% CL})$$

(Mainz & Troisk experiments)

– Katrin proposed to improve present sensitivity to  $m_{\text{eff}}^\beta \sim 0.3 \text{ eV}$

# Neutrino Mass Scale: Other Channels

## Muon neutrino mass

- From the two body decay at rest

$$\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$$

- Energy momentum conservation:

$$m_\pi = \sqrt{p_\mu^2 + m_\mu^2} + \sqrt{p_\mu^2 + m_\nu^2}$$

$$m_\nu^2 = m_\pi^2 + m_\mu^2 - 2 + m_\mu \sqrt{p^2 + m_\pi^2}$$

- Measurement of  $p_\mu$  plus the precise knowledge of  $m_\pi$  and  $m_\mu \Rightarrow m_\nu$
- The present experimental result bound:

$$m_{\nu_\mu}^{eff} \equiv \sum m_j |U_{\mu j}|^2 < 190 \text{ KeV}$$

## Tau neutrino mass

- The  $\tau$  is much heavier  $m_\tau = 1.776 \text{ GeV}$   
 $\Rightarrow$  Large phase space  $\Rightarrow$  difficult precision for  $m_\nu$

- The best precision is obtained from hadronic final states

$$\tau \rightarrow n\pi + \nu_\tau \quad \text{with } n \geq 3$$

- Lep I experiments obtain:

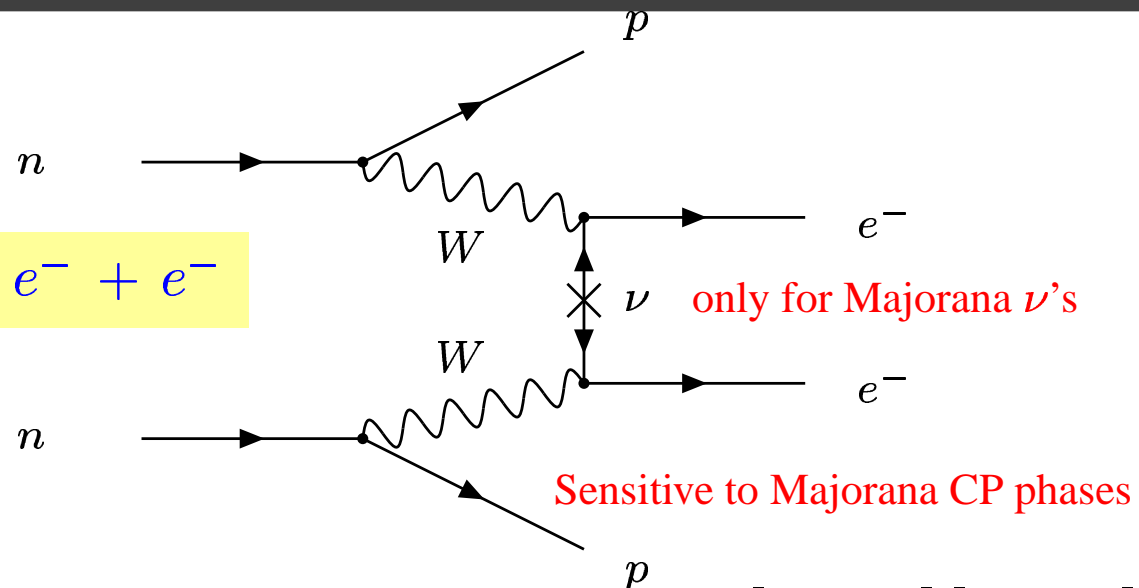
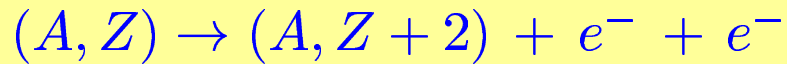
$$m_{\nu_\tau}^{eff} \equiv \sum m_j |U_{\tau j}|^2 < 18.2 \text{ MeV}$$

$\Rightarrow$  If mixing angles  $U_{ej}$  are not negligible

Best kinematic limit on Neutrino Mass Scale comes from Tritium Beta Decay



# Neutrino Mass Scale: $\nu$ -less Double- $\beta$ Decay



- Amplitude involves the product of two leptonic currents:  $[\bar{e}\gamma^\mu L\nu][\bar{e}\gamma^\mu L\nu]$

– If  $\nu$  Dirac  $\Rightarrow \nu$  annihilates a neutrino and creates an antineutrino

$\Rightarrow$  no same state  $\Rightarrow$  Amplitude = 0

– If  $\nu$  Majorana  $\Rightarrow \nu = \nu^c$  annihilates and creates a neutrino=antineutrino

$\Rightarrow$  same state  $\Rightarrow$  Amplitude  $\propto \overline{\nu}(\nu^c)^T \neq 0$

- Amplitude of  $\nu$ -less- $\beta\beta$  decay is proportional to  $|\langle m_{ee} \rangle| = \left| \sum U_{ej}^2 m_j \right|$

– Present bound:  $|\langle m_{ee} \rangle| < 0.35 \text{ eV}$  +theor. uncert.  $< 1.05 \text{ eV}$  (90% CL)

– Several proposed experiments to reach  $|\langle m_{ee} \rangle| \sim 10^{-2} \text{ eV}$

# Neutrino Mass Scale in Cosmology

$\sum m_{\nu_i}$  has effects on:

Cosmic Microwave  
Background Temperature  
Fluctuations

Most recent from WMAP

Large scale structure:

– 2° Field Galaxy

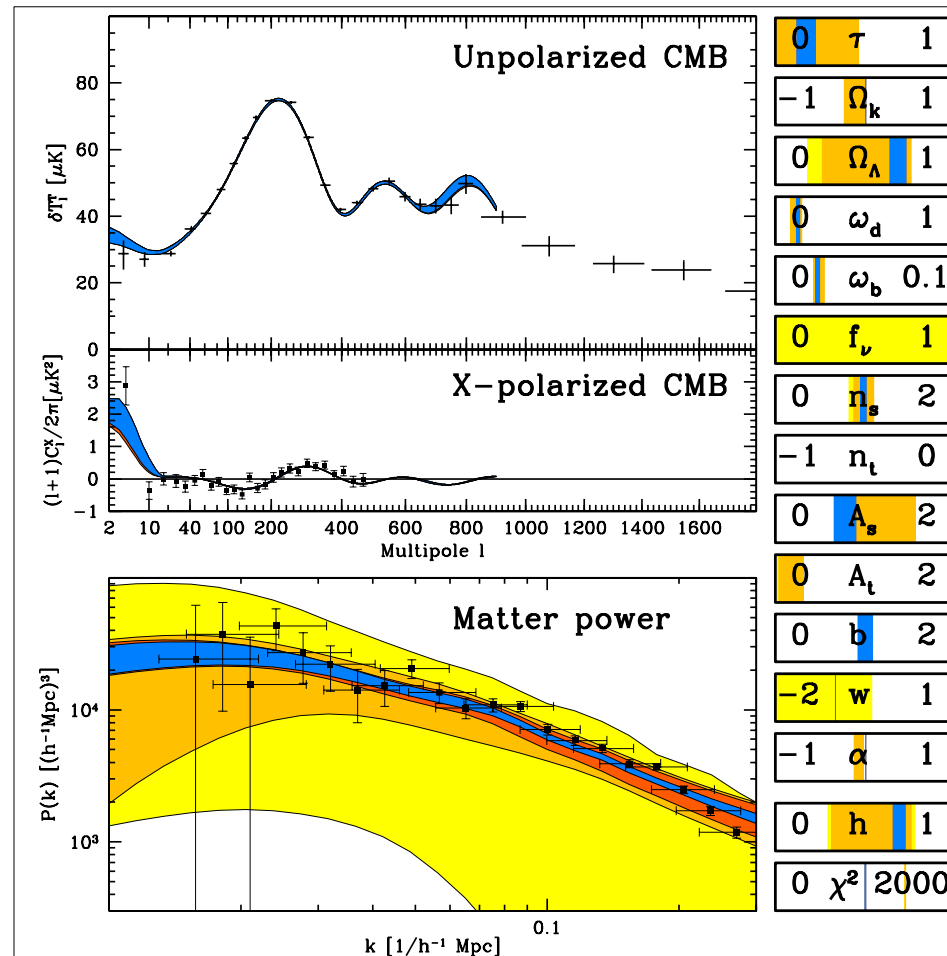
Redshift Survey

(2dFGRS)

– Sloan Digital

Sky Survey (SDSS)

⇒ limit on  $\sum m_{\nu_i}$  depends on  
prior and data used to constraint  
other 12 parameters



Tegmark *et. al* astro-ph/0310723

Problem: 13 parameters to be determined!!

$$\sum m_{\nu_i} \leq 0.7 - 2.1 \text{ eV} \text{ at } 95 \% \text{ CL}$$

# Summary I

- In the **SM**:
  - **Accidental** global symmetry:  $B \times L_e \times L_\mu \times L_\tau \leftrightarrow m_\nu \equiv 0$
  - neutrinos are **left-handed** ( $\equiv$  helicity -1):  $m_\nu = 0 \Rightarrow$  **chirality**  $\equiv$  **helicity**
  - No distinction between **Majorana** or **Dirac** Neutrinos
- If  $m_\nu \neq 0 \rightarrow$  Need to extend SM
  - $\rightarrow$  different ways of adding  $m_\nu$  to the SM
    - **breaking** total lepton number ( $L = L_e + L_\mu + L_\tau$ )  $\rightarrow$  **Majorana**  $\nu$ :  $\nu = \nu^C$
    - **conserving** total lepton number  $\rightarrow$  **Dirac**  $\nu$ :  $\nu \neq \nu^C$
  - $\rightarrow$  **Lepton Mixing**  $\equiv$  breaking of  $L_e \times L_\mu \times L_\tau$
- From direct searches of  $\nu$ -mass:  $m_\nu \leq \mathcal{O}(eV)$

Question: How to search for  $m_\nu \ll \mathcal{O}(eV)$ ?

Answer: **Tomorrow....**